| Domain: Number and Operations in Base Ten  | 3   | 4   | 5   |
|--|---|---|---|
| Use place value understanding and<br>properties of operations to perform<br>multi-digit arithmetic | 3.NBT.1<br>Use place value understanding to<br>round whole numbers to the nearest<br>10 or 100.   | 4.NBT.3<br>Use place value understanding to<br>round multi-digit whole numbers to<br>any place  | 5.NBT.4<br>Use place value understanding to<br>round decimals to any place.   |
|  | 3.NBT.2<br>Fluently add and subtract within 1000<br>using strategies and algorithms based<br>on place value, properties of<br>operations, and/or the relationship<br>between addition and subtraction.  | 4.NBT.4<br><b>Fluently</b> add and subtract multi-digit<br>whole numbers using the standard<br>algorithm.   | 5.NBT.5<br><b>Fluently</b> multiply multi-digit whole<br>numbers using the standard algorithm.  |
|  | 3.NBT.3<br>Multiply one-digit whole numbers by<br>multiples of 10 in the range 10-90<br>(e.g., $9 \times 80$ , $5 \times 60$ ) using strategies<br>based on place value and properties<br>of operations.  | 4.NBT.5<br>Multiply a whole number of up to four<br>digits by a one-digit whole number,<br>and multiply two two-digit numbers,<br>using strategies based on place value<br>and the properties of operations.<br>Illustrate and explain the calculation<br>by using equations, rectangular<br>arrays, and/or area models.  | 5.NBT.2<br>Explain patterns in the number of<br>zeros of the product when multiplying<br>a number by powers of 10, and<br>explain patterns in the placement of<br>the decimal point when a decimal is<br>multiplied or divided by a power of 10.<br>Use whole-number exponents to<br>denote powers of 10.   |
|  | 3.OA.2<br>Interpret whole-number quotients of<br>whole numbers, e.g., interpret 56 ÷ 8<br>as the number of objects in each<br>share when 56 objects are partitioned<br>equally into 8 shares, or as a number<br>of shares when 56 objects are<br>partitioned into equal shares of 8<br>objects each. For example, describe a<br>context in which a number of shares<br>or a number of groups can be<br>expressed as 56 ÷ 8. | 4.NBT.6<br>Find whole-number quotients and<br>remainders with up to four-digit<br>dividends and one-digit divisors, using<br>strategies based on place value, the<br>properties of operations, and/or the<br>relationship between multiplication<br>and division. Illustrate and explain the<br>calculation by using equations,<br>rectangular arrays, and/or area<br>models. | 5.NBT.6<br>Find whole-number quotients of whole<br>numbers with up to four-digit<br>dividends and two-digit divisors, using<br>strategies based on place value, the<br>properties of operations, and/or the<br>relationship between multiplication<br>and division. Illustrate and explain the<br>calculation by using equations,<br>rectangular arrays, and/or area<br>models. |

| Domain: Number and Operations in Base Ten  | 3 | 4   | 5   |
|--|---|---|---|
| Use place value understanding and<br>properties of operations to perform<br>multi-digit arithmetic     |   | 4.NF.5<br>Express a fraction with denominator<br>10 as an equivalent fraction with<br>denominator 100, and use this<br>technique to add two fractions with<br>respective denominators 10 and 100.<br>For example, express 3/10 as 30/100,<br>and add 3/10 + 4/100 = 34/100. | 5.NBT.7<br>Add, subtract, multiply, and divide<br>decimals to hundredths, using<br>concrete models or drawings and<br>strategies based on place value,<br>properties of operations, and/or the<br>relationship between addition and<br>subtraction; relate the strategy to a<br>written method and explain the<br>reasoning used. |
|  |   | 4.NF.6<br>Use decimal notation for fractions with<br>denominators 10 or 100. For example,<br>rewrite 0.62 as 62/100; describe a<br>length as 0.62 meters; locate 0.62 on<br>a number line diagram.  |   |
| Generalize place value<br>understanding for multi-digit whole<br>numbers and decimals to<br>hundredths |   | 4.NBT.1<br>Recognize that in a multi-digit whole<br>number, a digit in one place<br>represents ten times what it<br>represents in the place to its right. For<br>example, recognize that 700 ÷ 70 = 10<br>by applying concepts of place value<br>and division.              | 5.NBT.1<br>Recognize that in a multi-digit number,<br>a digit in one place represents 10<br>times as much as it represents in the<br>place to its right and 1/10 of what it<br>represents in the place to its left.   |
|  |   | 4.NBT.2<br>Read and write multi-digit whole<br>numbers using base-ten numerals,   | 5.NBT.3<br>Read, write, and compare decimals to thousandths.  |
|  |   | number names, and expanded form.<br>Compare two multi-digit numbers<br>based on meanings of the digits in<br>each place, using >, =, and < symbols<br>to record the results of comparisons.   | 5.NBT.3a<br>Read and write decimals to<br>thousandths using base-ten numerals,<br>number names, and expanded form,<br>e.g., $347.392 = 3 \times 100 + 4 \times 10 + 7 \times 1 + 3 \times (1/10) + 9 \times (1/100) + 2 \times (1/1000)$ .  |
| Domain: Number and Operations in   | 3 | 4   | 5   |

| Domain: Number and Operations in Base Ten  | 3  | 4  | 5   |
|--|--|--|---|
| Generalize place value<br>understanding for multi-digit whole<br>numbers and decimals to<br>hundredths |  | 4.NF.7<br>Compare two decimals to hundredths<br>by reasoning about their size.<br>Recognize that comparisons are valid<br>only when the two decimals refer to<br>the same whole. Record the results of<br>comparisons with the symbols >, =, or<br><, and justify the conclusions, e.g., by<br>using a visual model. | 5.NBT.3b<br>Compare two decimals to thousandths<br>based on meanings of the digits in<br>each place, using >, =, and < symbols<br>to record the results of comparisons  |
| Represent and solve problems<br>involving multiplication and<br>division.                              | 3.OA.4<br>Determine the unknown whole<br>number in a multiplication or division<br>equation relating three whole<br>numbers. For example, determine the<br>unknown number that makes the<br>equation true in each of the equations<br>$8 \times ? = 48, 5 = \_ \div 3, 6 \times 6 = ?$ |  | 5.OA.2<br>Write simple expressions that record<br>calculations with numbers, and<br>interpret numerical expressions<br>without evaluating them. For example,<br>express the calculation "add 8 and 7,<br>then multiply by 2" as 2 × (8 + 7).<br>Recognize that 3 × (18932 + 921) is<br>three times as large as 18932 + 921,<br>without having to calculate the<br>indicated sum or product. |
|  | 3.OA.6<br>Understand division as an unknown-<br>factor problem. <i>For example, find 32</i> ÷<br>8 by finding the number that makes 32<br>when multiplied by 8.  |  |   |
|  | 3.OA.3<br>Use multiplication and division within<br>100 to solve word problems in<br>situations involving equal groups,<br>arrays, and measurement quantities,<br>e.g., by using drawings and equations<br>with a symbol for the unknown<br>number to represent the problem            |  |   |

| Domain: Operations and Algebraic Thinking                                 | 3  | 4 | 5   |
|---|--|---|---|
| Represent and solve problems<br>involving multiplication and<br>division. | 3.OA.4<br>Determine the unknown whole<br>number in a multiplication or division<br>equation relating three whole<br>numbers. For example, determine the<br>unknown number that makes the<br>equation true in each of the equations<br>$8 \times ? = 48, 5 = \_ \div 3, 6 \times 6 = ?$ |   | 5.OA.2<br>Write simple expressions that record<br>calculations with numbers, and<br>interpret numerical expressions<br>without evaluating them. For example,<br>express the calculation "add 8 and 7,<br>then multiply by 2" as 2 × (8 + 7).<br>Recognize that 3 × (18932 + 921) is<br>three times as large as 18932 + 921,<br>without having to calculate the<br>indicated sum or product. |
|   | 3.OA.6<br>Understand division as an unknown-<br>factor problem. For example, find 32 ÷<br>8 by finding the number that makes 32<br>when multiplied by 8.   |   |   |
|   | 3.OA.3<br>Use multiplication and division within<br>100 to solve word problems in<br>situations involving equal groups,<br>arrays, and measurement quantities,<br>e.g., by using drawings and equations<br>with a symbol for the unknown<br>number to represent the problem            |   |   |

| Domain: Operations and Algebraic<br>Thinking   | 3  | 4  | 5   |
|--|--|--|---|
| Understand properties of<br>multiplication and the relationship<br>between multiplication and<br>division. | 3.OA.5<br>Apply properties of operations as<br>strategies to multiply and divide.<br><i>Examples:</i> If $6 \times 4 = 24$ is known, then<br>$4 \times 6 = 24$ is also known.<br>(Commutative property of<br>multiplication.) $3 \times 5 \times 2$ can be found<br>by $3 \times 5 = 15$ , then $15 \times 2 = 30$ , or by<br>$5 \times 2 = 10$ , then $3 \times 10 = 30$ .<br>(Associative property of<br>multiplication.) Knowing that $8 \times 5 =$<br>$40$ and $8 \times 2 = 16$ , one can find $8 \times 7$<br>as $8 \times (5 + 2) = (8 \times 5) + (8 \times 2) = 40$<br>+ 16 = 56. (Distributive property.) |  | 5.OA.1<br>Use parentheses, brackets, or braces<br>in numerical expressions, and<br>evaluate expressions with these<br>symbols |
|  | 3.OA.1<br>Interpret products of whole numbers,<br>e.g., interpret 5 × 7 as the total<br>number of objects in 5 groups of 7<br>objects each. For example, describe a<br>context in which a total number of<br>objects can be expressed as 5 × 7   | 4.OA.1<br>Interpret a multiplication equation as a<br>comparison, e.g., interpret 35 = 5 × 7<br>as a statement that 35 is 5 times as<br>many as 7 and 7 times as many as 5.<br>Represent verbal statements of<br>multiplicative comparisons as<br>multiplication equations |   |
| Multiply and divide within 100.  | 3.OA.7<br>Fluently multiply and divide within<br>100, using strategies such as the<br>relationship between multiplication<br>and division (e.g., knowing that $8 \times 5$<br>= 40, one knows $40 \div 5 = 8$ ) or<br>properties of operations. By the end<br>of Grade 3, know from memory all<br>products of two one-digit numbers.   |  |   |

| Domain: Operations and Algebraic Thinking   | 3  | 4   | 5 |
|---|--|---|---|
| Solve problems involving the four<br>operations, and identify and explain<br>patterns in arithmetic | 3.OA.8<br>Solve two-step word problems using<br>the four operations. Represent these<br>problems using equations with a letter<br>standing for the unknown quantity.<br>Assess the reasonableness of<br>answers using mental computation<br>and estimation strategies including<br>rounding                            | 4.OA.3<br>Solve multistep word problems posed<br>with whole numbers and having<br>whole-number answers using the four<br>operations, including problems in<br>which remainders must be interpreted.<br>Represent these problems using<br>equations with a letter standing for the<br>unknown quantity. Assess the<br>reasonableness of answers using<br>mental computation and estimation<br>strategies including rounding. |   |
|   | 3.OA.9<br>Identify arithmetic patterns (including<br>patterns in the addition table or<br>multiplication table), and explain them<br>using properties of operations. For<br>example, observe that 4 times a<br>number is always even, and explain<br>why 4 times a number can be<br>decomposed into two equal addends. | 4.OA.2<br>Multiply or divide to solve word<br>problems involving multiplicative<br>comparison, e.g., by using drawings<br>and equations with a symbol for the<br>unknown number to represent the<br>problem, distinguishing multiplicative<br>comparison from additive comparison.  |   |

| Domain: Operations and Algebraic<br>Thinking | 3 | 4  | 5  |
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|  |   |  |  |
| Gain familiarity with factors and multiples. |   | 4.OA.4<br>Find all factor pairs for a whole<br>number in the range 1-100. Recognize<br>that a whole number is a multiple of<br>each of its factors. Determine whether<br>a given whole number in the range 1-<br>100 is a multiple of a given one-digit<br>number. Determine whether a given<br>whole number in the range 1-100 is<br>prime or composite.  |  |
| Generate and analyze patterns.               |   | 4.OA.5<br>Generate a number or shape pattern<br>that follows a given rule. Identify<br>apparent features of the pattern that<br>were not explicit in the rule itself. For<br>example, given the rule "Add 3" and<br>the starting number 1, generate terms<br>in the resulting sequence and observe<br>that the terms appear to alternate<br>between odd and even numbers.<br>Explain informally why the numbers<br>will continue to alternate in this way. | 5.OA.3<br>Generate two numerical patterns<br>using two given rules. Identify<br>apparent relationships between<br>corresponding terms. Form ordered<br>pairs consisting of corresponding<br>terms from the two patterns, and<br>graph the ordered pairs on a<br>coordinate plane. For example, given<br>the rule "Add 3" and the starting<br>number 0, and given the rule "Add 6"<br>and the starting number 0, generate<br>terms in the resulting sequences, and<br>observe that the terms in one<br>sequence are twice the corresponding<br>terms in the other sequence. Explain<br>informally why this is so. |

| Develop understanding of fractions as numbers.       3.NF.1       Understand a fraction 1/b as the quantity formed by 1 part when a whole is partitioned into b equal parts; understand a fraction a/b as the quantity formed by a parts of size 1/b.       4.NF.1         S.NF.2       Understand a fraction as a number on the number line; represent fractions on a number line diagram.       4.NF.1         S.NF.2       Understand a fraction 1/b on a number line diagram by defining the interval from 0 to 1 as the whole and partitioning it into b equal parts.       4.NF.1 | Domain: Numbers and Operations-<br>Fractions | 3   | 4   | 5 |
|---|--|---|---|---|
| Recognize that each part has size 1/b<br>and that the endpoint of the part<br>based at 0 locates the number 1/b on<br>the number line.         3.NF.2b         Represent a fraction a/b on a number<br>line diagram by marking off a lengths<br>1/b from 0. Recognize that the<br>resulting interval has size a/b and that<br>its endpoint locates the number a/b on<br>the number line         3.NF.3         S.NF.3         Suplain equivalence of fractions in<br>special cases, and compare fractions<br>by reasoning about their size.   | Develop understanding of fractions           | Understand a fraction 1/b as the<br>quantity formed by 1 part when a<br>whole is partitioned into b equal parts;<br>understand a fraction a/b as the<br>quantity formed by a parts of size 1/b.<br>3.NF.2<br>Understand a fraction as a number on<br>the number line; represent fractions<br>on a number line diagram.<br>3.NF.2a<br>Represent a fraction 1/b on a number<br>line diagram by defining the interval<br>from 0 to 1 as the whole and<br>partitioning it into b equal parts.<br>Recognize that each part has size 1/b<br>and that the endpoint of the part<br>based at 0 locates the number 1/b on<br>the number line.<br>3.NF.2b<br>Represent a fraction a/b on a number<br>line diagram by marking off a lengths<br>1/b from 0. Recognize that the<br>resulting interval has size a/b and that<br>its endpoint locates the number a/b on<br>the number line<br>3.NF.3<br>Explain equivalence of fractions in<br>special cases, and compare fractions | Explain why a fraction $a/b$ is<br>equivalent to a fraction $(n \times a)/(n \times b)$<br>by using visual fraction models, with<br>attention to how the number and size<br>of the parts differ even though the two<br>fractions themselves are the same<br>size. Use this principle to recognize |   |

| Domain: Numbers and Operations-<br>Fractions      | 3   | 4  | 5 |
|---|---|--|---|
| Develop understanding of fractions<br>as numbers. | 3.NF.3a<br>Understand two fractions as<br>equivalent (equal) if they are the same<br>size, or the same point on a number<br>line  |  |   |
|   | 3.NF.3b<br>Recognize and generate simple<br>equivalent fractions, e.g., $1/2 = 2/4$ ,<br>4/6 = 2/3. Explain why the fractions<br>are equivalent, e.g., by using a visual<br>fraction model.   |  |   |
|   | 3.NF.3c<br>Express whole numbers as fractions,<br>and recognize fractions that are<br>equivalent to whole numbers.<br>Examples: Express 3 in the form 3 =<br>3/1; recognize that 6/1 = 6; locate 4/4<br>and 1 at the same point of a number<br>line diagram.  |  |   |
|   | 3.NF.3d<br>Compare two fractions with the same<br>numerator or the same denominator<br>by reasoning about their size.<br>Recognize that comparisons are valid<br>only when the two fractions refer to<br>the same whole. Record the results of<br>comparisons with the symbols >, =, or<br><, and justify the conclusions, e.g., by<br>using a visual fraction model. | 4.NF.2<br>Compare two fractions with different<br>numerators and different<br>denominators, e.g., by creating<br>common denominators or numerators,<br>or by comparing to a benchmark<br>fraction such as 1/2. Recognize that<br>comparisons are valid only when the<br>two fractions refer to the same whole.<br>Record the results of comparisons<br>with symbols >, =, or <, and justify the<br>conclusions, e.g., by using a visual<br>fraction model. |   |

| Domain: Numbers and Operations-<br>Fractions                                | 3 | 4  | 5   |
|---|---|--|---|
| Build fractions from unit fractions.  |   | 4.NF.3<br>Understand a fraction a/b with a > 1<br>as a sum of fractions 1/b.   |   |
| Use equivalent fractions as a<br>strategy to add and subtract<br>fractions. |   | 4.NF.3a<br>Understand addition and subtraction<br>of fractions as joining and separating<br>parts referring to the same whole  | 5.NF.1<br>Add and subtract fractions with unlike<br>denominators (including mixed<br>numbers) by replacing given fractions<br>with equivalent fractions in such a way<br>as to produce an equivalent sum or<br>difference of fractions with like<br>denominators. For example, $2/3 + 5/4$<br>= $8/12 + 15/12 = 23/12$ . (In general,<br>a/b + c/d = (ad + bc)/bd.) |
|   |   | 4.NF.3b<br>Decompose a fraction into a sum of<br>fractions with the same denominator<br>in more than one way, recording each<br>decomposition by an equation. Justify<br>decompositions, e.g., by using a<br>visual fraction model. Examples: $3/8 =$<br>1/8 + 1/8 + 1/8; $3/8 = 1/8 + 2/8$ ; $2 1/8= 1 + 1 + 1/8 = 8/8 + 8/8 + 1/8$ . |   |
|   |   | 4.NF.3c<br>Add and subtract mixed numbers with<br>like denominators, e.g., by replacing<br>each mixed number with an equivalent<br>fraction, and/or by using properties of<br>operations and the relationship<br>between addition and subtraction.   |   |

| Domain: Numbers and Operations-<br>Fractions                                   | 3 | 4  | 5  |
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| Use equivalent fractions as a<br>strategy to add and subtract<br>fractions.    |   | 4.NF.3d<br>Solve word problems involving<br>addition and subtraction of fractions<br>referring to the same whole and<br>having like denominators, e.g., by<br>using visual fraction models and<br>equations to represent the problem.  | 5.NF.2<br>Solve word problems involving<br>addition and subtraction of fractions<br>referring to the same whole, including<br>cases of unlike denominators, e.g., by<br>using visual fraction models or<br>equations to represent the problem.<br>Use benchmark fractions and number<br>sense of fractions to estimate mentally<br>and assess the reasonableness of<br>answers. For example, recognize an<br>incorrect result 2/5 + 1/2 = 3/7, by<br>observing that 3/7 < 1/2. |
| Apply and extend previous<br>understandings of multiplication<br>and division. |   | <ul> <li>4.NF.4</li> <li>Apply and extend previous<br/>understandings of multiplication to<br/>multiply a fraction by a whole number.</li> <li>4.NF.4a</li> <li>Understand a fraction a/b as a<br/>multiple of 1/b. For example, use a<br/>visual fraction model to represent 5/4<br/>as the product 5 × (1/4), recording the<br/>conclusion by the equation 5/4 = 5 ×<br/>(1/4).</li> </ul> | 5.NF.4<br>Apply and extend previous<br>understandings of multiplication to<br>multiply a fraction or whole number by<br>a fraction.  |
|  |   | 4.NF.4b<br>Understand a multiple of a/b as a<br>multiple of 1/b, and use this<br>understanding to multiply a fraction by<br>a whole number. For example, use a<br>visual fraction model to express $3 \times$<br>(2/5) as $6 \times$ (1/5), recognizing this<br>product as 6/5. (In general, $n \times (a/b) =$<br>( $n \times a$ )/b.)  | 5.NF.4a<br>Interpret the product (a/b) × q as a<br>parts of a partition of q into b equal<br>parts; equivalently, as the result of a<br>sequence of operations a × q $\div$ b. For<br>example, use a visual fraction model<br>to show (2/3) × 4 = 8/3, and create a<br>story context for this equation. Do the<br>same with (2/3) × (4/5) = 8/15. (In<br>general, (a/b) × (c/d) = ac/bd.)  |

| Domain: Numbers and Operations-<br>Fractions                                   | 3 | 4  | 5  |
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| Apply and extend previous<br>understandings of multiplication<br>and division. |   | 4.NF.4c<br>Solve word problems involving<br>multiplication of a fraction by a whole<br>number, e.g., by using visual fraction<br>models and equations to represent the<br>problem. For example, if each person<br>at a party will eat 3/8 of a pound of<br>roast beef, and there will be 5 people<br>at the party, how many pounds of<br>roast beef will be needed? Between<br>what two whole numbers does your<br>answer lie? | 5.NF.3<br>Interpret a fraction as division of the<br>numerator by the denominator (a/b = a<br>÷ b). Solve word problems involving<br>division of whole numbers leading to<br>answers in the form of fractions or<br>mixed numbers, e.g., by using visual<br>fraction models or equations to<br>represent the problem. For example,<br>interpret 3/4 as the result of dividing 3<br>by 4, noting that 3/4 multiplied by 4<br>equals 3, and that when 3 wholes are<br>shared equally among 4 people each<br>person has a share of size 3/4. If 9<br>people want to share a 50-pound sack<br>of rice equally by weight, how many<br>pounds of rice should each person<br>get? Between what two whole<br>numbers does your answer lie? |
|  |   |  | 5.F.4b<br>Find the area of a rectangle with<br>fractional side lengths by tiling it with<br>unit squares of the appropriate unit<br>fraction side lengths, and show that<br>the area is the same as would be<br>found by multiplying the side lengths.<br>Multiply fractional side lengths to find<br>areas of rectangles, and represent<br>fraction products as rectangular areas   |
|  |   |  | 5.F.5a<br>Interpret multiplication as scaling<br>(resizing), by Comparing the size of a<br>product to the size of one factor on the<br>basis of the size of the other factor,<br>without performing the indicated<br>multiplication.   |

| Domain: Numbers and Operations-<br>Fractions                                   | 3 | 4 | 5   |
|--|---|---|---|
| Apply and extend previous<br>understandings of multiplication<br>and division. |   |   | 5.NF.5b<br>Explaining why multiplying a given<br>number by a fraction greater than 1<br>results in a product greater than the<br>given number (recognizing<br>multiplication by whole numbers<br>greater than 1 as a familiar case);<br>explaining why multiplying a given<br>number by a fraction less than 1<br>results in a product smaller than the<br>given number; and relating the<br>principle of fraction equivalence $a/b =$<br>$(n \times a)/(n \times b)$ to the effect of<br>multiplying a/b by 1. |
|  |   |   | 5.NF.6<br>Solve real world problems involving<br>multiplication of fractions and mixed<br>numbers, e.g., by using visual fraction<br>models or equations to represent the<br>problem.   |
|  |   |   | 5.NF.7<br>Apply and extend previous<br>understandings of division to divide<br>unit fractions by whole numbers and<br>whole numbers by unit fractions   |
|  |   |   | 5.NF.7a<br>Interpret division of a unit fraction by a<br>non-zero whole number, and compute<br>such quotients. For example, create a<br>story context for $(1/3) \div 4$ , and use a<br>visual fraction model to show the<br>quotient. Use the relationship between<br>multiplication and division to explain<br>that $(1/3) \div 4 = 1/12$ because $(1/12) \times 4 = 1/3$ .   |

| Domain: Numbers and Operations-<br>Fractions                                  | 3 | 4 | 5  |
|---|---|---|--|
| Apply and extend previous<br>understandings of multiplication<br>and division |   |   | <ul> <li>5.NF.7b</li> <li>Interpret division of a whole number<br/>by a unit fraction, and compute such<br/>quotients. For example, create a story<br/>context for 4 ÷ (1/5), and use a visual<br/>fraction model to show the quotient.<br/>Use the relationship between<br/>multiplication and division to explain<br/>that 4 ÷ (1/5) = 20 because 20 × (1/5)<br/>= 4.</li> <li>5.NF.7c</li> <li>Solve real world problems involving<br/>division of unit fractions by non-zero<br/>whole numbers and division of whole<br/>numbers by unit fractions, e.g., by<br/>using visual fraction models and<br/>equations to represent the problem.<br/>For example, how much chocolate will<br/>each person get if 3 people share 1/2<br/>lb of chocolate equally? How many<br/>1/3-cup servings are in 2 cups of<br/>raisins?</li> </ul> |

| Domain: Measurement and Data   | 3   | 4  | 5  |
|--|---|--|--|
| Solve problems involving<br>measurement and estimation.                    | 3.MD.1<br>Tell and write time to the nearest<br>minute and measure time intervals in<br>minutes. Solve word problems<br>involving addition and subtraction of<br>time intervals in minutes, <i>e.g., by</i><br><i>representing the problem on a number</i><br><i>line diagram</i>   |  |  |
|  | 3.MD.2<br>Measure and estimate liquid volumes<br>and masses of objects using standard<br>units of grams (g), kilograms (kg), and<br>liters (l).1 Add, subtract, multiply, or<br>divide to solve one-step word<br>problems involving masses or<br>volumes that are given in the same<br>units, e.g., by using drawings (such as<br>a beaker with a measurement scale)<br>to represent the problem. |  |  |
| Solve problems involving<br>measurement and conversion of<br>measurements. |   | 4.MD.1<br>Know relative sizes of measurement<br>units within one system of units<br>including km, m, cm; kg, g; lb, oz.; l,<br>ml; hr, min, sec. Within a single<br>system of measurement, express<br>measurements in a larger unit in terms<br>of a smaller unit. Record<br>measurement equivalents in a two-<br>column table. For example, know that<br>1 ft is 12 times as long as 1 in.<br>Express the length of a 4 ft snake as<br>48 in. Generate a conversion table for<br>feet and inches listing the number<br>pairs (1, 12), (2, 24), (3, 36), | 5.MD.1<br>Convert among different-sized<br>standard measurement units within a<br>given measurement system (e.g.,<br>convert 5 cm to 0.05 m), and use<br>these conversions in solving multi-<br>step, real world problems. |

| Domain: Measurement and Data  | 3  | 4  | 5   |
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| Solve problems involving<br>measurement and conversion of<br>measurements |  | 4.MD.2<br>Use the four operations to solve word<br>problems involving distances, intervals<br>of time, liquid volumes, masses of<br>objects, and money, including<br>problems involving simple fractions or<br>decimals, and problems that require<br>expressing measurements given in a<br>larger unit in terms of a smaller unit.<br>Represent measurement quantities<br>using diagrams such as number line<br>diagrams that feature a measurement<br>scale. |   |
|   |  | 4.MD.3<br>Apply the area and perimeter formulas<br>for rectangles in real world and<br>mathematical problems. For example,<br>find the width of a rectangular room<br>given the area of the flooring and the<br>length, by viewing the area formula as<br>a multiplication equation with an<br>unknown factor.   |   |
| Represent and interpret data.   | 3.MD.3<br>Draw a scaled picture graph and a<br>scaled bar graph to represent a data<br>set with several categories. Solve<br>one- and two-step "how many more"<br>and "how many less" problems using<br>information presented in scaled bar<br>graphs. For example, draw a bar<br>graph in which each square in the bar<br>graph might represent 5 pets. | 4.MD.4<br>Make a line plot to display a data set<br>of measurements in fractions of a unit<br>(1/2, 1/4, 1/8). Solve problems<br>involving addition and subtraction of<br>fractions by using information<br>presented in line plots. For example,<br>from a line plot find and interpret the<br>difference in length between the<br>longest and shortest specimens in an<br>insect collection.   | 5.NF.2<br>Make a line plot to display a data set<br>of measurements in fractions of a unit<br>(1/2, 1/4, 1/8). Use operations on<br>fractions for this grade to solve<br>problems involving information<br>presented in line plots. For example,<br>given different measurements of liquid<br>in identical beakers, find the amount<br>of liquid each beaker would contain if<br>the total amount in all the beakers<br>were redistributed equally. |

| Domain: Measurement and Data   | 3  | 4 | 5  |
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| Represent and interpret data   | 3.MD.4<br>Generate measurement data by<br>measuring lengths using rulers<br>marked with halves and fourths of an<br>inch. Show the data by making a line<br>plot, where the horizontal scale is<br>marked off in appropriate units—<br>whole numbers, halves, or quarters. |   |  |
| Geometric measurement:<br>understand concepts of area and<br>relate area to multiplication and to<br>addition. | 3.MD.5<br>Recognize area as an attribute of<br>plane figures and understand<br>concepts of area measurement.   |   | 5.MD.3<br>Recognize volume as an attribute of<br>solid figures and understand concepts<br>of volume measurement.   |
| Geometric measurement:<br>understand concepts of volume.   | 3.MD.5a<br>A square with side length 1 unit, called<br>"a unit square," is said to have "one<br>square unit" of area, and can be used<br>to measure area.  |   | 5.MD.3a<br>A cube with side length 1 unit, called a<br>"unit cube," is said to have "one cubic<br>unit" of volume, and can be used to<br>measure volume. |
|  | 3.MD.5b<br>A plane figure which can be covered<br>without gaps or overlaps by n unit<br>squares is said to have an area of n<br>square units.  |   | 5.MD.3b<br>A solid figure which can be packed<br>without gaps or overlaps using n unit<br>cubes is said to have a volume of n<br>cubic units.            |
|  | 3.MD.6<br>Measure areas by counting unit<br>squares (square cm, square m,<br>square in, square ft, and improvised<br>units)  |   | 5.MD.4<br>Measure volumes by counting unit<br>cubes, using cubic cm, cubic in, cubic<br>ft, and improvised units.  |

| Domain: Measurement and Data                             | 3  | 4 | 5   |
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| Geometric measurement:<br>understand concepts of volume. | 3.MD.7<br>Relate area to the operations of<br>multiplication and addition.   |   | 5.MD.5<br>Relate volume to the operations of<br>multiplication and addition and solve<br>real world and mathematical problems<br>involving volume   |
|  | 3.MD.7a<br>Find the area of a rectangle with<br>whole-number side lengths by tiling it,<br>and show that the area is the same as<br>would be found by multiplying the side<br>lengths.   |   | 5.MD.5q<br>Find the volume of a right rectangular<br>prism with whole-number side lengths<br>by packing it with unit cubes, and<br>show that the volume is the same as<br>would be found by multiplying the<br>edge lengths, equivalently by<br>multiplying the height by the area of<br>the base. Represent threefold whole-<br>number products as volumes, e.g., to<br>represent the associative property of<br>multiplication. |
|  | 3.MD.7b<br>Multiply side lengths to find areas of<br>rectangles with whole-number side<br>lengths in the context of solving real<br>world and mathematical problems,<br>and represent whole-number products<br>as rectangular areas in mathematical<br>reasoning |   | 5.MD.5b<br>Apply the formulas V = I × w × h and V<br>= b × h for rectangular prisms to find<br>volumes of right rectangular prisms<br>with whole-number edge lengths in<br>the context of solving real world and<br>mathematical problems.  |
|  | 3.MD.7c<br>Use tiling to show in a concrete case<br>that the area of a rectangle with<br>whole-number side lengths a and b +<br>c is the sum of a × b and a × c. Use<br>area models to represent the<br>distributive property in mathematical<br>reasoning.      |   |   |

| Domain: Measurement and Data  | 3  | 4   | 5   |
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| Geometric measurement:<br>understand concepts of volume.                      | 3.MD.7d<br>Recognize area as additive. Find<br>areas of rectilinear figures by<br>decomposing them into non-<br>overlapping rectangles and adding the<br>areas of the non-overlapping parts,<br>applying this technique to solve real<br>world problems.   |   | 5.MD.5c<br>Recognize volume as additive. Find<br>volumes of solid figures composed of<br>two non-overlapping right rectangular<br>prisms by adding the volumes of the<br>non-overlapping parts, applying this<br>technique to solve real world<br>problems. |
|   |  |   | 5.MD.3<br>Recognize volume as an attribute of<br>solid figures and understand concepts<br>of volume measurement.  |
| Geometric measurement: recognize<br>perimeter.                                | 3.MD.8<br>Solve real world and mathematical<br>problems involving perimeters of<br>polygons, including finding the<br>perimeter given the side lengths,<br>finding an unknown side length, and<br>exhibiting rectangles with the same<br>perimeter and different areas or with<br>the same area and different<br>perimeters. |   |   |
| Geometric measurement:<br>understand concepts of angle and<br>measure angles. |  | 4.MD.5<br>Recognize angles as geometric<br>shapes that are formed wherever two<br>rays share a common endpoint, and<br>understand concepts of angle<br>measurement: |   |

| Domain: Measurement and Data  | 3 | 4   | 5 |
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| Geometric measurement:<br>understand concepts of angle and<br>measure angles. |   | 4.MD.5a<br>An angle is measured with reference<br>to a circle with its center at the<br>common endpoint of the rays, by<br>considering the fraction of the circular<br>arc between the points where the two<br>rays intersect the circle. An angle that<br>turns through 1/360 of a circle is<br>called a "one-degree angle," and can<br>be used to measure angles.   |   |
|   |   | 4.MD.5b<br>An angle that turns through n one-<br>degree angles is said to have an<br>angle measure of n degrees.  |   |
|   |   | 4.MD.6<br>Measure angles in whole-number<br>degrees using a protractor. Sketch<br>angles of specified measure.  |   |
|   |   | 4.MD.7<br>Recognize angle measure as additive.<br>When an angle is decomposed into<br>non-overlapping parts, the angle<br>measure of the whole is the sum of<br>the angle measures of the parts.<br>Solve addition and subtraction<br>problems to find unknown angles on a<br>diagram in real world and<br>mathematical problems, e.g., by using<br>an equation with a symbol for the<br>unknown angle measure. |   |

| Domain: Geometry  | 3   | 4   | 5   |
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| Reason with shapes and their attributes.  | 3.G.1<br>Understand that shapes in different<br>categories (e.g., rhombuses,<br>rectangles, and others) may share<br>attributes (e.g., having four sides), and<br>that the shared attributes can define a<br>larger category (e.g., quadrilaterals).<br>Recognize rhombuses, rectangles,<br>and squares as examples of<br>quadrilaterals, and draw examples of<br>quadrilaterals that do not belong to<br>any of these subcategories. |   | 5.G.3<br>Classify two-dimensional figures into<br>categories based on their properties. |
|   | 3.G.2<br>Partition shapes into parts with equal<br>areas. Express the area of each part<br>as a unit fraction of the whole. For<br>example, partition a shape into 4 parts<br>with equal area, and describe the area<br>of each part as 1/4 of the area of the<br>shape.  |   |   |
| Draw and identify lines and angles,<br>and classify shapes by properties<br>of their lines and angles |   | 4.G.1<br>Draw points, lines, line segments,<br>rays, angles (right, acute, obtuse), and<br>perpendicular and parallel lines.<br>Identify these in two-dimensional<br>figures. |   |

| Domain: Geometry  | 3 | 4   | 5  |
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| Draw and identify lines and angles,<br>and classify shapes by properties<br>of their lines and angles |   | 4.G.2<br>Classify two-dimensional figures<br>based on the presence or absence of<br>parallel or perpendicular lines, or the<br>presence or absence of angles of a<br>specified size. Recognize right<br>triangles as a category, and identify<br>right triangles. |  |
| Domain: Geometry  | 3 | 4   | 5  |
| Graph points on the coordinate<br>plane to solve real-world and<br>mathematical problems.             |   | 4.G.3<br>Recognize a line of symmetry for a<br>two-dimensional figure as a line<br>across the figure such that the figure<br>can be folded along the line into<br>matching parts. Identify line-symmetric<br>figures and draw lines of symmetry.                  |  |
|   |   |   | . 5.G.1<br>Understand that the first number<br>indicates how far to travel from the<br>origin in the direction of one axis, and<br>the second number indicates how far<br>to travel in the direction of the second<br>axis, with the convention that the<br>names of the two axes and the<br>coordinates correspond (e.g., x-axis<br>and x-coordinate, y-axis and y-<br>coordinate). |

| Domain: Geometry  | 3 | 4 | 5   |
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| Graph points on the coordinate plane to solve real-world and mathematical problems. |   |   | 5.G.4<br>Classify two-dimensional figures in a<br>hierarchy based on properties   |
|   |   |   | 5.G.2<br>Represent real world and<br>mathematical problems by graphing<br>points in the first quadrant of the<br>coordinate plane, and interpret<br>coordinate values of points in the<br>context of the situation. |